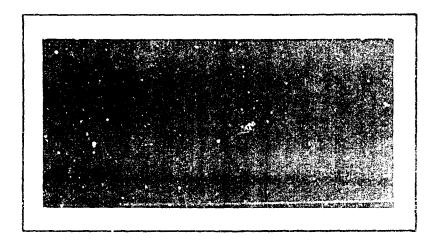
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# AIR UNIVERSITY UNITED STATES AIR FORCE



SCHOOL OF ENGINEERING

WRIGHT-PATTERSON AIR FORCE BASE, OHIO



THE LATTICE PARAMETERS OF SIX BINARY TITANIUM ALLOYS AT CRYOGENIC TEMPERATURES

THESIS

GAW/MC/68-8 Roy G. Inness, Jr. Capt USAF

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## THE LATTICE PARAMETERS OF SIX BINARY TITANIUM ALLOYS AT CRYOGENIC TEMPERATURES

#### THESIS

Presented to the Faculty of the School of Engineering of the Air Force Institute of Technology

Air University

in Partial Fulfillment of the Requirements for the Degree of

Master of Science

by

Roy G. Inness, Jr., B.S.

Capt

USAF

Graduate Aerospace Weapons

June 1968

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#### Preface

This thesis presents the results of an experimental determination of the lattice parameters for six titanium alloys over the temperature range 300° to 5°K. It is hoped that this additional information, however small, will be of some value in the extensive investigation of the materials available for man's use.

It would have been impossible to complete this invostigation without the aid and effort of many individuals.

In acknowledgment, I wish to express my appreciation to the following people: Lt. Colonel Edward J. Myers, thesis advisor, for teaching me the fundamentals of x-ray diffraction and for his counsel and advise during this study;

Dr. Barold Gedel, thesis sponsor, for making available the materials and equipment used in this study; Capt. Wilbur Simmons for his introduction to the computer program used;

Mr. Paul Vincent for annealing the powder samples; Mr.

Ken Storey for his timely supply of liquid helium; and Miss Sally Allen for typing this thesis.

pinally, my special thanks to Mr. Gene Charles whose operational knowledge of x-ray diffraction procedures and assistance in the day-to-day experiments were invaluable.

Roy G. Inness, Jr.

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#### List of Symbols

- A Angstrom unit (1 x 108 cm)
- "a" Lattice parameter (spacing between atoms in the basal plane)
- "c" Lattice parameter (spacing between basal planes)
- 20 Angle between the incident x-ray beam and the reflected x-ray beam
- (hk·l) Indices of a crystal plane (used to identify the recorded x-ray peaks)

Front-reflection region - 20 < 90°

Back-reflection region - 20 > 90°

#### Abstract

The lattice parameters of six binary titanium alloys (3.10Al, 4.99Al, 2.11V, 4.04V, 1.37Sn, and 2.56Sn) were determined over the temperature range 300° to 5°K. 29 values were measured using the powder x-ray diffraction technique; cryogenic temperatures were obtained by using liquid helium and liquid nitrogen. Lattice parameters were calculated by the analytical least-squares extrapolation technique, using a computer program for the actual calculations.

Both the "a" and "c" lattice parameters decreased linearly from 300°K to a "break point" between 125° and 100°K. The "a" lattice parameter then continued to decrease, at a reduced rate, from the "break point" to 5°K. Below the "break point" the "c" lattice parameter either remained constant or continued to decrease at a reduced rate, depending on the alloy.

The linear coefficients of thermal expansion were calculated over the temperature ranges of 300° to 125°K and 100° to 5°K.

## THE LATTICE PARAMETERS OF SIX BINARY TITANIUM ALLOYS AT CRYOGENIC TEMPERATURES

#### I. Introduction

Frequently, requirements have often demanded that new materials be used operationally before a complete knowledge and explanation of their properties and behavior are known. Titanium alloys are now one of the most widely used of these new materials. This has led to an extensive research program to record and explain the properties and behavior of titanium, particularly at the extreme temperatures that it must withstand. A recent study has shown that there is a definite break in the approximately linear decrease of the lattice parameters of pure titanium, occuring near 100°K (Ref 3).

As part of the continuing investigation of titanium, at cryogenic temperatures, the primary purpose of this study was to determine the lattice parameters of six titanium alloys over a temperature range of 300° (room temperature) to 5°K. A secondary purpose was to determine if there was any correlation between the alloying element (amount and type) and the behavior of the lattice parameters at low temperatures. This study was conducted at the Air Force Materials Laboratory, Wright-Patterson AFB, Ohio.

Throughout this thesis, the x-ray peaks (lines) are identified by the (hk·l) value of the reflecting crystal plane, and all 20 values are for resolved copper F21 radiation. All lattice parameters are for the hexagonal crystal structure phase of titanium. Though some betatitanium may have been present in the Ti-4.04V alloy, no x-ray peaks for this phase were observed.

This thesis is organized into five major sections:

(1) Experimental Materials, (2) Experimental Equipment and Procedures, (3) Data Analysis, (4) Results, and (5) Conclusions. Supplementary information is included in the appendixes, and a list of symbols is included on page vi.

#### II. Experimental Materials

#### Titanium Alloys

Six binary titanium alloy samples were supplied by the Douglas Missile and Space Division of the Douglas Aircraft Company. The six alloys were, by weight percent: Ti-3.10Al, Ti-4.99Al, Ti-2.11V, Ti-4.04V, Ti-1.37Sn, and Ti-2.56Sn. The iron, nitrogen, oxygen, and carbon contents of each alloy were also furnished by Douglas and are listed in Appendix C. Each alloy was a high-purity sample prepared from iodide titanium and was in sheet form, approximately 0.035-inches thick.

#### Preparation of Powder Samples

Powder samples, which expose many randomly-oriented grains to the x-ray beam, will normally produce a satisfactory x-ray pattern. Therefore, an annealed 325-mesh powder sample was prepared from each titanium alloy sheet. The powder was prepared by first filing a sheet until a sufficient quantity of filings was obtained. A permanent magnet was then passed over the filings to remove any particles of iron chipped from the file. The filings were then hand ground with a mortar and pestle until the resulting powder would pass through a 325-mesh screen.

The initial attempt to hand grind the filings indicated that it would be a tedious and time consuming process to grind a powder sample for each alloy. Filings from one alloy were then placed in a mechanical shaker which utilized an iron cup and steel-ball bearings. After a 15-minute run the magnet was passed over the resulting powder, and it picked up almost all of the powder. It appeared that most of the titanium had become imbedded on the steel balls and the powder was mostly iron particles from the cup, so this method of powder preparation was discarded. Next, in an attempt to reduce the ductility of the titanium, a strip was cut from one of the titanium alloy sheets and cold-rolled until about a 50% reduction in thickness was achieved. This reduced the ductility enough to allow a sufficient quantity of powder from one sheet to be prepared in about four hours, by hand grinding filings from the cold-rolled strip in the mortar and pestle.

A 325-mesh powder sample was then prepared from each alloy sheet. The file was cleaned throughly with acetone and a file brush after filing each alloy, and the mortar and pestle were cleaned with hydrochloric acid to dissolve any smeared titanium before grinding a different alloy.

A complete scan was then run on one of the unannealed powder samples. All peaks above  $2\theta = 90^{\circ}$  were absent and the peaks in the front-reflection region appeared weak and broad. This resulted from the severe cold-working during powder preparation. The Ti-1.37Sn powder sample was then encapsulated in pure titanium foil and vacuum

annealed (10<sup>-7</sup> torr) for 10 hours at 650°C. A complete scan of the annealed powder showed all peaks with an intensity greater than five, as compared to an intensity of 100 for the (01.1) peak, were present. However, the peaks in the back-reflection region were still somewhat broad, being up to one and one-half degrees wide. In an attempt to increase their quality, the Ti-4.99Al powder was annealed under the same conditions, but for 24 hours. This longer annealing time resulted in such a minute increase in quality that the remaining four powder samples were vacuum annealed (10<sup>-7</sup> torr) for 10 hours at 650°C. A higher annealing temperature was not tried because a small amount of sintering occurred at 650°C. It was known that sintering becomes a problem at higher temperatures (Ref 3:6). Before annealing, each powder sample was washed in acetone to remove any light foreign particles introduced during preparation.

Finally, after annealing, the diamond powder that was needed to align the cryogenic attachment was added to each powder sample. The diamond powder was obtained by washing 45-micron commercial diamond grinding paste in acetone until the diamond powder separated. An approximate ratio of one-part diamond powder to three-parts titanium powder was used.

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#### III. Experimental Equipment and Procedures

#### Cryogenic Temperatures

A Materials Research Corporation Model X-86GC lowtemperature, high-vacuum attachment, designed for use with the General Electric SPG spectrogoniometer, was used to obtain the cryogenic temperatures. It consists basically of an inner and outer dewar, a copper sample mounting stage, and a base unit (see Figure 8). A carbon-resistance thermometer and a copper-constantan thermocouple are built into the rear face of the copper stage for temperature measurements. It also has a built-in heating element for temperature variation. The base unit has provisions for translation along the x-axis and rotation about the y-axis and the z-axis. This allows the copper stage to be aligned with the focusing circle of the spectrogoniometer. The areas around the sample stage, between the two dewars, and around the outer dewar were evacuated to 10<sup>-5</sup> torr.

A powder-sample temperature of 5°K was obtained by filling the outer dewar with liquid nitrogen and the inner dewar with liquid helium. 40°K was obtained by using the heater element. However, use of the heating element greatly increased the evaporation rate of the helium. This allowed only about 45 minutes at 5°K and 45 minutes at 40°K before all of the helium evaporated. This time was just sufficient to align the low-temperature attach-

ment and slow scan all the desired peaks. 85°K was obtained by filling both the inner and outer dewars with liquid nitrogen. The heating element was then used to obtain 100°, 125°, and 160°K. 200° and 250°K were obtained by removing the liquid nitrogen from the inner dewar and using the heating element.

The carbon-resistance thermometer was used to measure the 5°K temperature, and the copper-constantan thermocouple was used for 85°K and higher. Both devices were used for 40°K. The carbon resistance was measured with a Wheatstone bridge, and the thermocouple output by a Leads and Northrup 8686 millivolt potentiometer. The thermocouple reference junction that is located at the electrical connector pins on the base of the dewar is supposed to be at room temperature. However, cold liquid nitrogen gas that was boiling off from the outer dewar was cooling the reference junction. The actual temperature of the reference junction was determined by taping a laboratory-type mercury thermometer bulb next to the connector pins.

The 40°K temperature measurement was the most inaccurate, as the calibration curves for both temperature measuring devices are flat in this range (Ref 3:30). The two temperature-measuring devices were within 3°K of each other for this temperature, and it is considered accurate to \*2°K. All other temperatures are considered accurate

to \*1°K, being limited by the accuracy of the reference junction temperature. All temperature readings were recorded to the nearest degree.

#### X-Ray Diffraction

A General Electric XRD-5 x-ray unit, SPG spectrogoniometer, and SPG-3 detector were used. The basic spectrogoniometer is considered accurate to ±0.002°. The detector unit utilizes a xenon-filled proportional counter tube, and the diffraction peaks were recorded on a G.E. millivolt recorder strip chart. Nickel filtered copper radiation, with a Ka<sub>1</sub> wavelength (lamda) of 1.54050Å, was used. The x-ray tube was operated at 50,000 volts and 31 milliamps for all runs.

A powder sample was mounted on the copper sample stage face by using an acetone slurry and rotating the stage until the sample spread evenly. After the desired temperature was obtained, the cryogenic attachment was aligned. All alignment was done using the diamond (111) Kal peak located at 20 = 43.93°. This 20 value was calculated using a diamond lattice parameter value of 3.5667Å (Ref 1). Since the 20 shift for this diamond peak is only about +0.006° at 5°K (Ref 5), 43.93° was used for alignment at all temperatures. Alignment was accomplished by setting the diffractometer to 43.93° and adjusting the axes controls of the X-86GC base until the recorder pen peaked out. The diamond peak was then slow scanned using

a high-resolution technique (1° beam slit and 0.05° detector slit) and a 0.5-second time constant. The alignment was accepted if the diamond peak was located within \*0.01° of 43.93°. After alignment the axes-locking screws on the X-86GC base were tightened. This prevented any minor rotation of the cryogenic attachment about the z-axis because of the tension of the vacuum line as the diffractometer was scanning. Each time the temperature was changed the cryogenic attachment was re-aligned.

Because of the time limitation at low temperatures and the need to scan as many peaks as possible for the extrapolation technique, a schedule of time constants, beam and detector slits, scanning speeds, and peaks of acceptable quality was determined after considerable experimentation at room temperature. The eight best peaks above 20 = 60° were determined and scanned for all samples, except for the (21.3) peak of the titaniumaluminum alloys, which merged with the (331) diamond peak. As the 20 values of the peaks increased, the time constant had to be increased in order to get a smooth trace with the recorder pen. A 2-second time constant was used for the (11.0), (10.3), (11.2), and (20.1) peaks, a 4-second time constant for the (20.3) and (21.1) peaks, and a 8-second time constant for the (11.4) and (21.3)peaks. In the back-reflection region a low-resolution

technique (3° beam slit and 0.2° detector slit) was required to obtain satisfactory intensity of the x-ray peaks. The increased quality of the peaks in the front-reflection region allowed use of a higher-resolution technique (3° beam slit and 0.1° detector slit). All peaks were scanned using a 0.4° per minute diffractometer scalining speed and 500 counts per second on the recorder scale.

The selected peaks for each alloy were scanned, using the above conditions, at nine selected temperatures. The 20 values were then determined from the strip-chart record and the appropriate time-constant correction (discussed on page 11). Appendix A lists the corrected 20 values for each alloy and temperature.

#### IV. Data Analysis

#### Time-Constant Correction

All measured 29 values were corrected for the timeconstant lag in the recorder. The correction, for each
time constant used, was determined by slow scanning one
of the diamond peaks backward and forward seven times.
By comparing the mean 20 value for the forward scans with
the mean 20 value for the backward scans, the time-constant
lag for a forward scan only was determined. The resulting
corrections for a 2, 4, and 8-second time constant were
0.02°, 0.03°, and 0.04°, respectively. The time-constant
correction was added to the measured 20 value.

#### Calculation of Lattice Parameters

There are two basic methods for calculating accurate lattice parameters. Both have been developed to eliminate most of the systematic errors in the measured 20 values, such as absorption, eccentricity, and divergence. The first method uses an internal standard to obtain the 20 correction factors for systematic errors. The second method extrapolates the lattice parameter values to 0 = 90°, where theoretically all systematic errors vanish. In the second method, the values of the computed lattice parameters are plotted as the ordinate, and the abscissa is the corresponding value of a trigonometric function of 0.

A simple and very direct internal-standard method is to use the diamond powder, that was added to each alloy powder sample, as an internal standard (Ref 3:12). Using this technique, only two titanium peaks and one diamond peak (located near each other in the back-reflection region) have to be scanned. By comparing where the diamond peak is located relative to where it should be located, the systematic errors in the titanium 20 values can be rapidly determined. This method also alloys "a" and "c" to be readily calculated from a simultaneous solution of the hexagonal interplanar spacing equations for the two titanium peaks scanned. However, this method was not used because of the following reasons: (1) the poor quality of the (30.2) titanium peak located near 149°, (2) the merging of the (21.3) peak of the titaniumaluminum alloys with the (331) diamond peak, rendering the (21.3) peak useless for measurements, (3) the doubt about the actual shift of the (331) diamond peak below 100°K (Ref 5).

Therefore, Cohen's extrapolation method was used to calculate the lattice parameters (Ref 4:467). This method is an analytical, least-squares extrapolation of "a" and "c" to  $\theta = 90^{\circ}$ . A trigonometric function of  $\theta$ , rather than  $\theta$  itself, is used to provide for linear extrapolation. The extrapolation to  $\theta = 90^{\circ}$  eliminates most of the systematic errors, while the least-squares method mini-

mizes the random errors. While Cohen's method will yield excellent results, the number of calculations becomes overwhelming when a large number of "a" and "c" values are determined. This was overcome by using, a readily available, but apparently seldom used, computer program to determine the lattice parameters (Ref 6). This program is a computerized version of Cohen's method. Inputs are the measured 20 values, the corresponding (hk·l) values, the desired weighting for each 20 value, the wavelength of the radiation used, the type of crystal system, and the desired extrapolation function. Outputs are the values of the lattice parameters and the probable error for each lattice parameter.

Once the raw data (20 values) are measured, the only variables to be selected by the user of the program are the extrapolation function and the weight given to each 20 value. Two of the more commonly used extrapolation functions are:

$$\frac{1}{2} \left( \frac{\cos^2 \theta}{\sin \theta} + \frac{\cos^2 \theta}{\theta} \right)$$
 (Nelson and Riley) (2)

henceforth referred to as  $F_1$  and  $F_2$  respectively. When peaks in the front-reflection region are used,  $F_2$  will usually result in a more accurate extrapolation of the lattice parameters (Ref 4:464). However, since these extrapolation functions were developed for the Debye-Scherrer photographic method and the computer program

allowed rapid determination of the lattice parameters, a comparison of F<sub>1</sub> and F<sub>2</sub> was undertaken. The room temperature lattice parameters of Ti-4.99Al, Ti-1.37Sn, and Ti-2.56Sn, and the lattice parameters of Ti-3.10Al from 300° to 5°K were calculated using each of the above extrapolation functions.

All "a" and "c" values calculated with  $F_2$  were consistently  $0.0002\text{\AA}$  to  $0.0003\text{\AA}$  lower than those calculated with  $F_1$ . However, the probable error using  $F_1$  was always lower, usually about  $0.0002\text{\AA}$ , than the probable error using  $F_2$ . This lower probable error indicated that the extrapolation was more linear when  $F_1$  was used. All lattice parameters in this thesis were calculated using  $F_1$ .

Initially, a weight of one was used for each 20 value. This led to slightly erratic results, since a small random error in the measured 20 value for a low-angle peak seriously affected the extrapolated lattice parameter. (Ref 2:324). This effect was partially eliminated by giving a weight of two to all 20 values in the back-reflection region and a weight of one to all 20 values in the front-reflection region. Thus, the lattice parameters were calculated using a computerized version of Cohen's analytical least-squares extrapolation method, with  $\cos^2\theta$  as the extrapolation function and a double weight given to the back-reflection 20 values. All com-

puter runs were done on an IBM 7094 computer.

#### Accuracy

The main items that must be considered in assessing the accuracy of the computed lattice parameters are:

(1) the diffractiometer, (2) alignment of the cryogenic attachment, (3) temperature measurements, (4) quality of the peaks, (5) alloy analysis, and (6) the probable error output of the computer program. The first three items were considered in Section III. The quality of the peaks varied progressively, from excellent in the low angle front-reflection region to poor in the extreme back-reflection region. Appraising the combined effect of the first four items, the measured 20 values are considered accurate to \*0.01° in the front-reflection region and \*0.02° in the back-reflection region.

Since the chemical analysis of each alloy was done before the powder samples were prepared, the exact chemical analysis of the powder samples is really unknown. All practical care was taken to prevent any contamination (especially by oxygen and nitrogen) during the preparation of the powder samples. However, the observation that the calculated room temperature "c" values for all six titanium alloys were larger than most previously reported values (see Appendix E) indicates that there may have been a small amount of oxygen and/or nitrogen contamination in the powder samples. It is known that only 0.5 weight per

cent oxygen increases the value of the "c" lattice parameter by approximately 0.008Å (Ref 7:1010).

For each lattice parameter calculated, the computer program also calculated a statistical probable error.

The probable errors are listed in Appendix B. This probable error was a 50% confidence interval, defined (for a normalized distribution) as 0.675 times the standard deviation. The mean of the probable errors for all "a" lattice parameter values calculated was \*0.0004Å.

The mean of the probable errors for all "c" lattice parameter values calculated was \*0.0007Å.

#### V. Results

#### Discussion

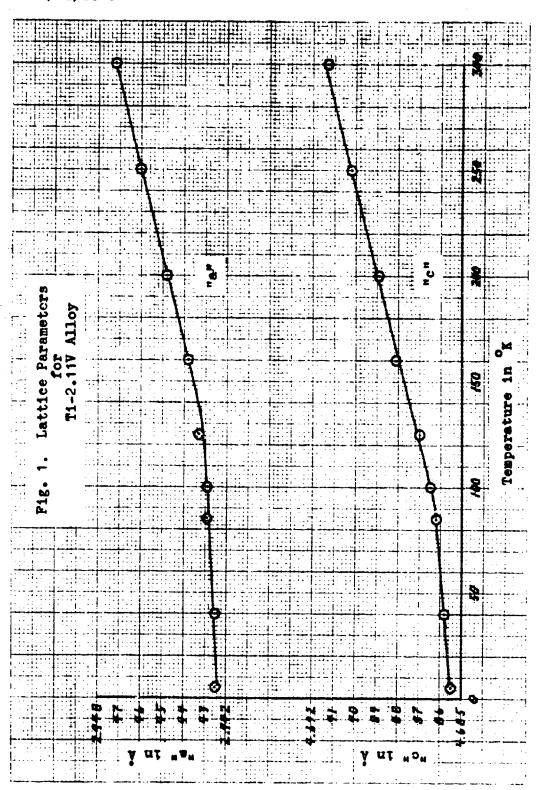
The calculated lattice parameters for each alloy, plotted as function of temperature, are presented in Figures 1 to 6. The c/a ratios, calculated from values taken from the curves, are presented in Figure 7.

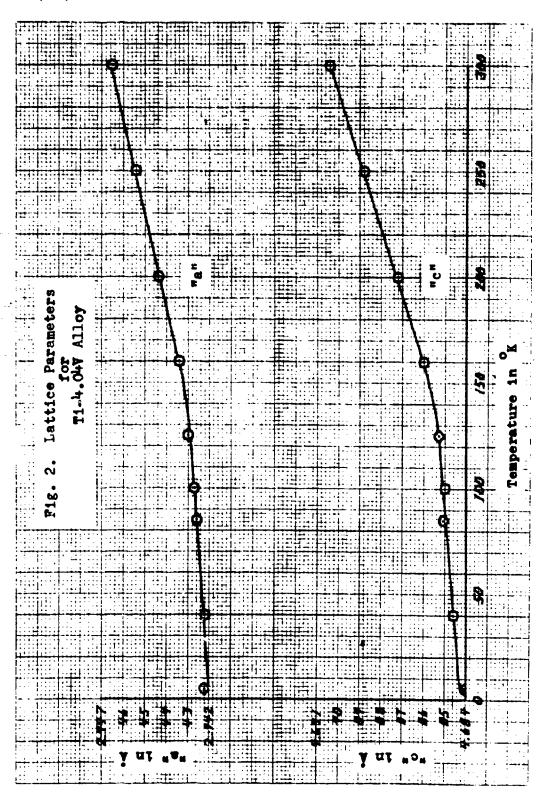
The calculated room temperature "a" value for each of the six titanium alloys was in good agreement with previously reported values. The calculated room temperature "c" value for each of the six titanium alloys was somewhat larger than most previously reported values, possibly due to oxygen and/or nitrogen contamination during preparation of the powder samples. Appendix E contains a comparison of the room temperature lattice parameters calculated in this thesis with previously reported values.

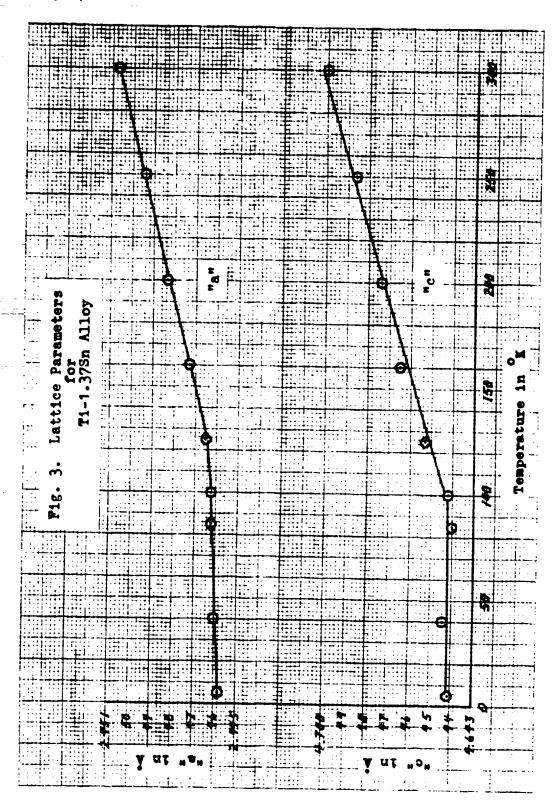
Appendix E also indicates the effect of alloying on the room temperature lattice parameters. By comparing the atomic radius of titanium with that of aluminum, tin, and vanadium it can be readily seen that the size factor is primarily determining whether the lattice parameters of pure titanium are increased or decreased when alloyed with these elements. However, the effect of relative valence and electronegativity must also be considered to explain any deviation from Vegard's Law (varying in linear proportion to size (Ref 7:23).

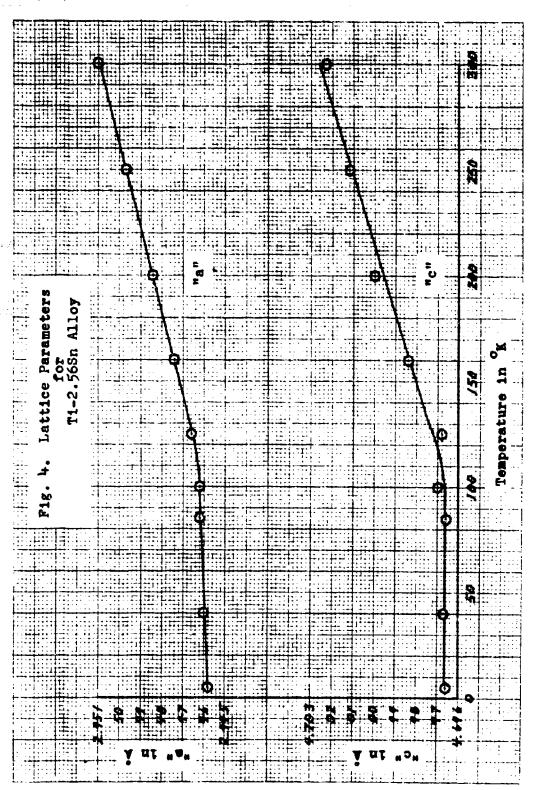
Essentially, the lattice parameters of all six alloys behaved the same at low temperatures. Both "a" and "c" decreased linearly to a "break point" between 125° and 100°K. Below the "break point" the "a" lattice parameter continued to decrease, at a reduced rate, for all alloys. Below the "break point" the "c" lattice parameter either remained constant or continued to decrease at a reduced rate, depending on the alloy.

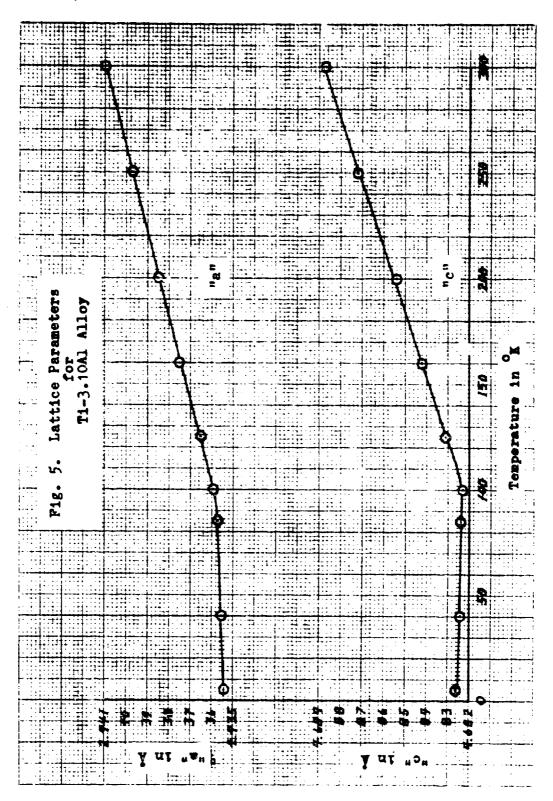
The "break point" between 125° and 100°K and the somewhat unusual behavior of the "c" lattice parameter below the "break point" confirms the results of Ebneter (Ref 3). While the exact cause of the "break point" and the somewhat unusual behavior of the "c" lattice parameter below the "break point" is unknown, Zwikker relates this type of behavior to the values and behavior of the Debye characteristic temperature, the low temperature specific heat constant, and lattice vibrations (Ref 8:144-167).

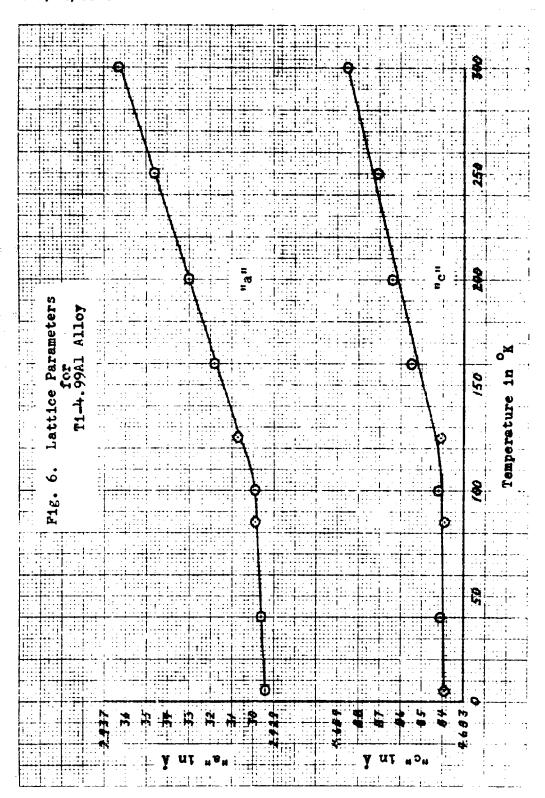


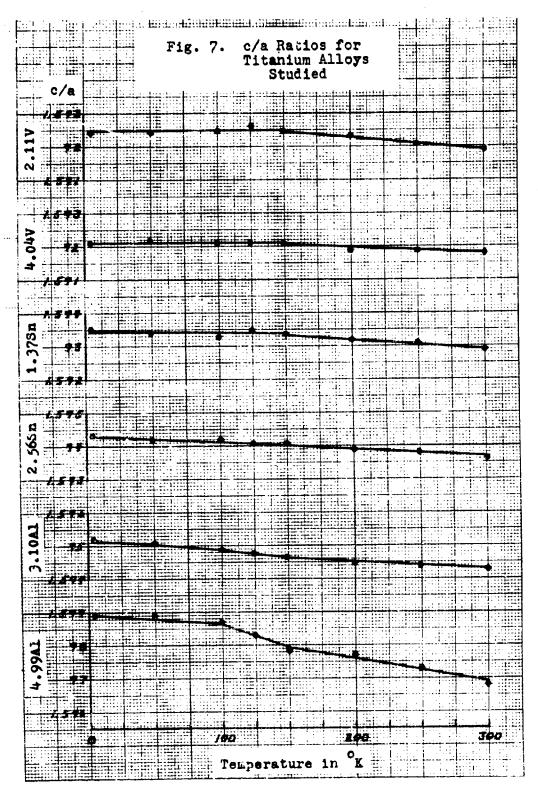












#### Coefficients of Expansion

A linear coefficient of thermal expansion was calculated for each alloy over the temperature ranges of 300° to 125°K and 100° to 5°K using the expression:

$$\alpha = \frac{1}{T_1 - T_2} \left\{ \frac{2\Delta a}{3 a} + \frac{\Delta c}{3 c} \right\} \tag{3}$$

where  $\alpha$  = linear coefficient of thermal expansion (per °C)

T<sub>1</sub> = upper temperature in °K

T<sub>2</sub> = lower temperature in °K

a = lattice parameter "a" at temperature T,

 $\Delta a = \text{change in lattice parameter "a" from T<sub>1</sub> to T<sub>2</sub>$ 

c = lattice parameter "c" at temperature T<sub>1</sub>

 $\Delta c$  = change in lattice parameter "c" from  $T_1$  to  $T_2$ The results are presented in the table below.

Table I Linear Coefficients of Thermal Expansion (Multiply by:  $10^{-6}/^{\circ}\text{C}$ )

Alloy	300° to 125°K	100° to 5°K
2.11V	7.1	1.9
4.04V	6.9	2.5
1.37Sn	7.4	1.0
2.56Sn	7.8	1.0
3.10Al	8.1	1.1
4.99Al	8.9	1.3

#### VI. Conclusions

- 1. There is a "break point" in the linear decrease of the lattice parameters, located between 125° and 100°K.
- 2. Below the "break point" the "a" lattice parameter continues to decrease, but at a reduced rate.
- 3. Below the "break point" the "c" lattice parameter remains nearly constant for the titanium-aluminum and the titanium-tin alloys and decreases at a reduced rate for the titanium-vanadium alloys.

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## Appendix A

## Raw Data (20 Values)

The following tables contain the measured 29 values for each alloy and temperature. All listed values have been corrected for the time-constant lag.

hkl

300°K

Table II Raw Data, Ti-2.11V Alloy 20 in Degrees

200°K

160°K

125°K

110	62.97	63.01	63.04	63.07	63.08
103	70.57	70.59	70.60	70.61	70.61
112	76.21	76.24	76.25	76.27	76.29
201	77.42	77.45	77.48	77.50	77.51
203	102.29	102.35	102.42	102.46	102.47
211	109.17	109.26	109.32	109.37	109.39
114	114.13	114.19	114.24	114.28	114.32
213	139.49	139.60	139.70	139.79	139.86
hkl 110 103 112 201 203 211 114 213	100°K 63.08 70.62 76.30 77.52 102.48 109.40 114.33 139.91	85°K 63.08 70.62 76.30 77.52 102.48 109.40 114.34 139.92	40°K 63.09 70.63 76.31 77.53 102.49 109.41 114.35 139.97	5°K 63.10 70.63 76.32 77.53 102.49 109.41 114.36 139.98	

250°K

Table III

Raw Data, Ti-4.04V Alloy

26 in Degrees

hkl	300°K	250°K	200°K	160°K	125°K
110 103 112 201 203 211 114 213	63.02 70.55 76.25 77.46 102.33 109.21 114.18 139.57	63.04 70.57 76.27 77.48 102.39 109.29 114.25 139.66	63.06 70.58 76.28 77.49 102.45 109.35 114.31 139.74	63.08 70.58 76.29 77.50 102.49 109.40 114.36 139.82	63.09 70.59 76.30 77.51 102.49 109.41 114.38 139.88
hk1	100°K	85°K	40°K	5 <b>°</b> K	
110	63.10	63.10	63.10	63.10	
103	70.59	70.59	70.60	70.60	
112	76.31	76.31	76.31	76.32	
201	77.51	77.51	77.52	77.52	
203	102.50	102.49	102.50	102.51	
211	109.42	109.42	109.43	109.43	
114	114.39	114.39	114.40	114.41	
213	139.92	139.93	139.99	140.00	

Table IV

# Raw Data, Ti-1.37Sn Alloy 20 in Degrees

hkl	300°K	250°K	200°K	160°K	125°K
110	62.85	62.89	62.93	62.97	62.99
103	70.31	70.33	70.39	70.39	70.41
112	76.04	76.07	76.10	76.13	76.14
201	77.25	77.29	77.33	77.36	77.39
203	102.06	102.12	102.18	102.22	102.26
211	108.94	109.02	109.09	109.15	109.20
	113.83	113.90	113.96	114.01	
114			139.26	139.35	139.43
213	139.05	139.16	139.20	139.33	137.43
hkl	100°K	85 <b>°</b> K	40°K	5 <b>°</b> K	
110	63.00	63.01	63.00	62.99	
103	70.42	70.41	70.42	70.41	
112	76.15	76.16	76.16	76.17	
201	77.41	77.42	77.42	77.41	
	102.29	102.30	102.29	102.30	
203		102.30	109.22	109.23	
211	109.21	114.10	114.09	114.10	
114	114.09				
213	139.48	139.48	139.49	139.50	

Table V

# Raw Data, Ti-2.56Sn Alloy 20 in Degrees

hk1	300°K	250°K	200°K	160°X	125°K
110	62.85	62.89	62.92	62.96	62.98
103	70.28	70.31	70.34	70.36	70.38
112	76.02	76.05	76.07	76.09	76.11
201	77,26	77.30	77.33	77.36	77.38
203	102.03	102.09	102.16	102.20	102.25
211	108.93	109.01	109.08	109.14	109.19
114	113.78	113.84	113.89	113.96	114.02
213	138.98	139.09	139.21	139.30	139.38

hkl	100°K	85°K	40°K	5 ° K
1.10	62,99	62.99	62.99	62.99
103	70.38	70.38	70.38	70.38
112	76.12	76.12	76.13	76.13
201	77.40	77.41	77.41	77.42
203	102.22	102.23	102.23	102.23
211	109.20	109.20	109.21	109.22
114	114.03	114.04	114.04	114.05
213	139.43	139.44	139.45	139.46

Table VI
Raw Data, Ti-3.10Al Alloy
20 in Degrees

hk1	300°K	250°K	200°K	160°K	125°X
110	63.12	63,15	63.18	63.20	63.22
103	70.58	70.61	70.65	70.67	70.70
112	76.37	76.41	76.44	76.46	76.49
201	77.60	77.63	77.67	77.70	77.72
203	102.55	102.61	102.67	102.71	102.74
211	109.50	109.57	109.64	109.69	109.75
114	114.33	114.39	114.46	114.51	114.56

hkl	100°K	85°K	40°K	5°K
110	63.23	63.24	63.24	63.25
103	70.71	70.71	70.70	70.71
112	76.50	76.51	76.52	76.51
201	77.74	77.74	77.75	77.76
203	102.77	102.78	102.78	102.78
211	109.78	109.79	109.80	109.81
114	114.59	114.59	114.60	114.60

Table VII

# Raw Data, Ti-4.99Al Alloy

## 20 in Degrees

300°K	250°K	200°K	160°K	125°K
63.3Q	63.34	63.39	63.42	63.45
70.67	70.70	70.74		70.80
76.49	76.53			76.65
77.79	77.84			77.98
102.69	102.76			102.90
109.78	109.87			110,10
114.48	114.55			114.73
100°K	85°K	40°K	5°K	
63.47	63.47	63.48	63.48	
70.81				
76.57	76.67			
77,99	77.99			
102.91	102.91	102.92		
110.15	110.15	110.16		
114.75	114.76	114.76	114.77	
	63.3Q 70.67 76.49 77.79 102.69 109.78 114.48 100°K 63.47 70.81 76.57 77.99 102.91 110.15	63.3Q 63.34 70.67 70.70 76.49 76.53 77.79 77.84 102.69 102.76 109.78 109.87 114.48 114.55	63.3Q 63.34 63.39 70.67 70.70 70.74 76.49 76.53 76.58 77.79 77.84 77.90 102.69 102.76 102.80 109.78 109.87 109.97 114.48 114.55 114.62  100°K 85°K 40°K 63.47 63.47 63.48 70.81 70.81 70.80 76.57 76.67 76.68 77.99 77.99 78.00 102.91 102.91 110.15 110.15 110.16	63.3Q 63.34 63.39 63.42 70.67 70.70 70.74 70.77 76.49 76.53 76.58 76.63 77.79 77.84 77.90 77.94 102.69 102.76 102.80 102.85 109.78 109.87 109.97 110.04 114.48 114.55 114.62 114.67  100°K 85°K 40°K 5°K 63.47 63.47 63.48 63.48 70.81 70.81 70.80 70.80 76.67 76.67 76.68 76.68 77.99 77.99 78.00 78.01 102.91 102.91 102.92 102.93 110.15 110.15 110.16 110.17

Appendix B
Probable Error in "a" and "c" Values

	Ti-2.11V			Ti-4.04V	
Temp	"a"	"c"	Temp	"a"	"c"
(°K)	(Å)	(Å)	(°K)	(Å)	(A)
300	0.0004	0.0006	300	0.0004	0.0007
250	0.0003	0.0005	250	0.0003	0.0005
200	0.0002	0.0003	200	0.0003	0.0005 0.0007
160	0.0002	0.0003	160	0.0005 0.0004	0.0007
125	0.0002	0.0003	125 100	0.0004	0.0006
100	0.3002	0.0004 0.0004	85	0.0004	0.0007
85	0.0003 0.0004	0.0004	40	0.0004	0.0007
40 5	0.0004	0.0007	5	0.0004	0.0007
	Ti-1.378	in.		Ti-2.56S	n
<b></b>	"a"	"c"	Temp	"a"	"c"
Temp	•	(ř.	(°K)	(Å)	(A)
(°K)	(A)				
300	0.0004	0.00.0	300	0.0004 0.0004	0.0007 c.0006
250	0.0004	0.0006	250 200	0.0003	0.0005
200	0.0004	0.0006 0.0006	160	0.0004	0.0007
160	0.0004 0.0004	0.0007	125	0.0005	0.0008
125 100	0.0005	0.0007	100	0.0006	0.0009
85	0.0006	0.0009	85	0.0006	c.0010
40	0.0004	0.0007	40	0.0006	0.0009
5	0.0005	0.0007	5	0.0006	0.0010
	Ti-3.10	Al		Ti-4.99	Al
Temp	"a"	"c"	Temp	"a"	"c"
(°K)	(A)	(Å)	(°K)	(Å)	(Å)
		0.0007	300	0.0004	0.0006
300	0.0004	0.0007	250	0.0004	0.0006
250 200	0.0004	0,0006	200	0.0005	0.0008
160	0.0004	0.0006	160	0.0005	0.0008
125	0.0002	0.0001	125	0.0005	0.0008
100	0.0002	0,0004	100	0.0006	0.0009 0.0010
85	0.0003	0.0005	85 40	0.0006	0.0010
40	0.0003	0,0006 0.0004	¥0 5	0.0006	0.0010
5	0.0002	0.0004	3		

## Appendix C

### Alloy Analysis

# Weight Percent

<u>Ti-2.11V</u>	<u>Ti-4.04V</u>
0.075 Fe	0.035 Fe
0.007 N <sub>2</sub>	0.006 N <sub>2</sub>
0.024 C	0.026 C
0.094 O <sub>2</sub>	0.090 O <sub>2</sub>
•	~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~

Ti-1.37Sn	Ti-2.56Sn
0.027 Fe	0.030 Fe
0.008 N <sub>2</sub>	0.006 N <sub>2</sub>
0.024 C	0.024 C
0.093 O <sub>2</sub>	0.072 O <sub>2</sub>

Ti-4.99A]		
0.089 Fe		
0.005 N <sub>2</sub>		
0.024 C		
0.104 02		

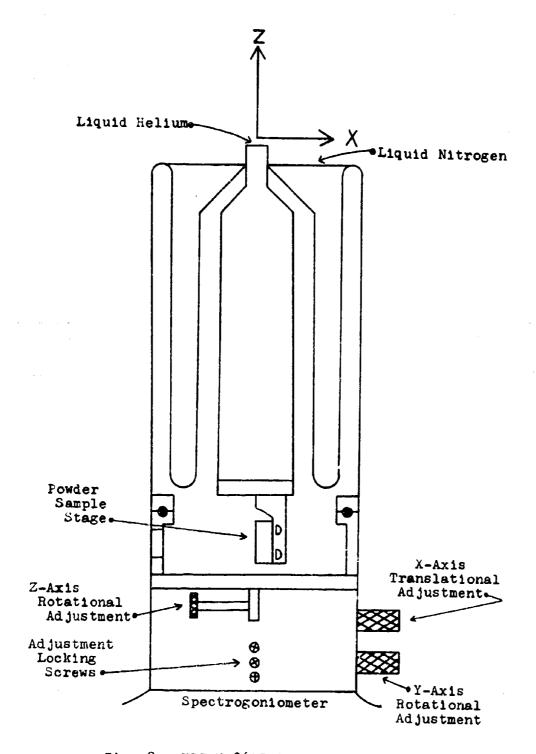
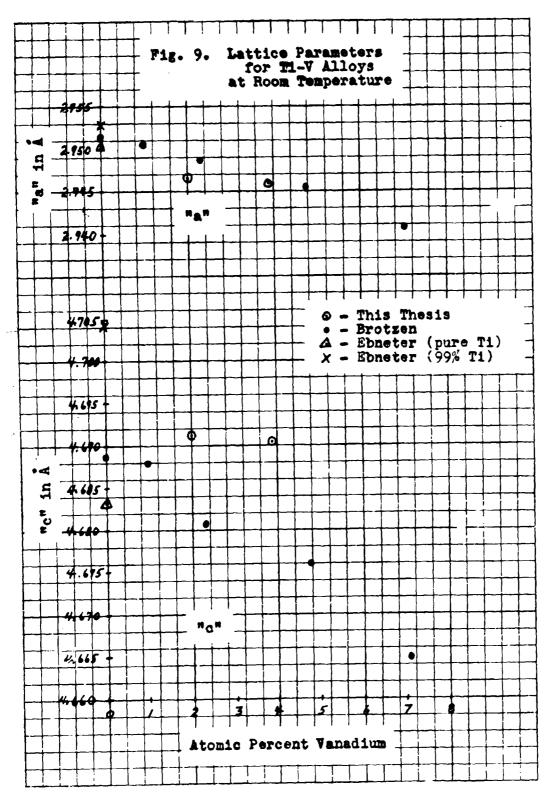


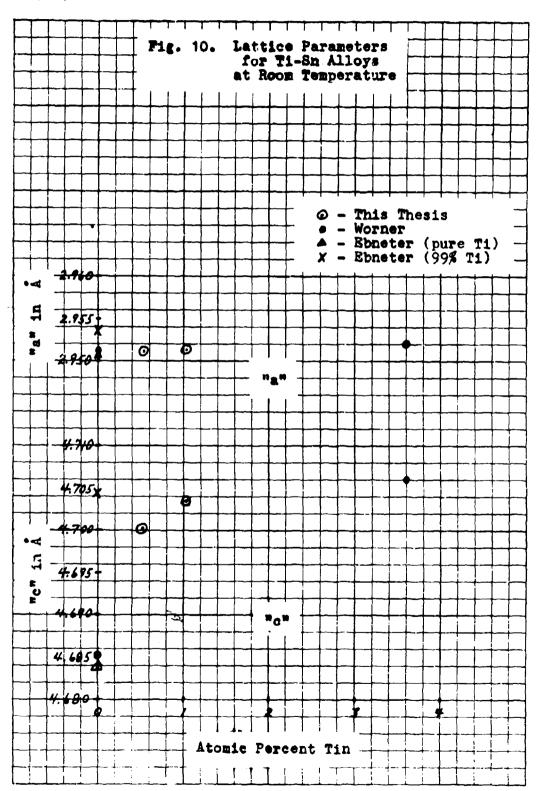
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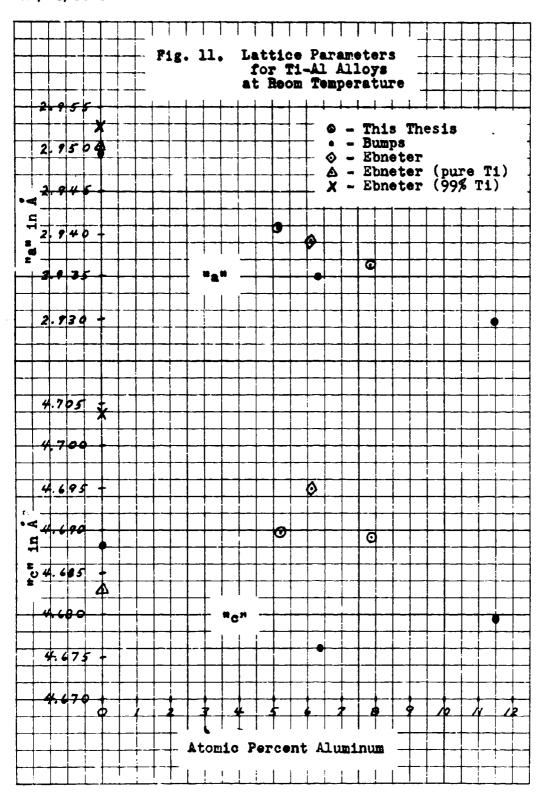
#### Appendix E

# Lattice Parameters for Titanium Alloys at Room Temperature

Presented in the following tables are the room temperature lattice parameter values calculated in this study and by other investigators. Ebneter's values are from reference 3, and all other values are from reference 7.







#### Vita

Roy George Inness, Jr. was born 1 October 1937 in Donaldsonville, Louisiana, the son of Roy George Inness and Rosemary Allen Inness. He graduated from Ascension High School in 1955 and received his Bachelor of Science degree from the United States Air Force Academy in 1959. After completing pilot training and F-100 advanced flying school, he was assigned to the 615th Tactical Fighter Squadron (F-100) at England AFB, Louisiana. In January 1963 he was assigned to the 416th Tactical Fighter Squadron at Misawa AB, Japan. He redeployed with the 416th Tactical Fighter Squadron to England AFB, Louisiana in June 1964 and to the Republic of Vietnam in November 1965. After completing 217 combat missions in Vietnam, he was assigned to AFIT in August 1966.

Permanent address: 318 Lee Avenue

Donaldsonville, Louisiana
This thesis was typed by Miss Sally Allen.

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